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Discrete Mathematics

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Chapter Two

SET THEORY

Section 2.1

Sets

Definition:

A set is a collection of objects, **the objects** in given set are called **elements** or **numbers of the set**.

" $x \in A$ " : denotes that x is an elements of the set A.

Example:

If A is the set of all integer and $x = 3, x \in A$.

Definition:

Two sets A and B are equal if they contain the same elements.

Example:

$$\begin{aligned} A &= \{ 1, 2, 3 \} \\ B &= \{ 1, 2, 2, 3, 3 \} \\ A &= B \end{aligned}$$

Definition:

If a set \acute{S} contains one element \acute{S} then we called it a **singleton** set.

Example:

$$\begin{aligned} \acute{S} &= \{ 1 \} \\ B &= \{ 0 \} \\ C &= \{ y \} \end{aligned} \quad \left. \begin{array}{l} \\ \\ \end{array} \right\} \text{ are singleton sets}$$

Let $A = \{ 2, 4, 6, 8, \dots \}$ then A is the set of all even natural numbers

$B = \{ 1, 3, 5, 7, \dots \}$ then B is the set of all odd natural numbers

Set – Builder Notation

Is a method to denote the numbers of a set A.

To do this we need a predicate $P(x)$ so that an element x is in A if $P(x)$ is true.

$$A = \{ x: x = 2n \text{ for some integers } n \}$$

$$\acute{S} = \{ x: \underbrace{x = P(x) \text{ is true}}_{P(x)} \}$$

Builder Notation

$$X = \{ x: x \text{ is real number and } 2 < x < 5 \} = (2, 5)$$

$$Y = \{ x: x \text{ is natural numbers divisible by } 5 \} Y = \{ 5, 10, 15, 20, \dots \}$$

Example:

$$A = \{ x: x \text{ is even prime number} \} = \{ 2 \}$$

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